

Limits Outline
AB Calculus I -- Spring 1995
Dr. Hartzler

2.1 Calculator explorations

Fact: $\lim_{x \rightarrow 0} \frac{\sin x}{x} = 1$

Limits: left/right/both for functions (p. 49 25-30)

Pictorial/graph limits left/right/both (p. 49 31-40)

Piecewise (p. 49 41-46)

2.2 Definition of a limit of a function as $x \rightarrow a$

“Proof” (example 1, pp. 54-55). We identified these steps:

1. Task statement
2. ϵ -tolerance statement
3. Work to $|x - a| < g(\epsilon)$ form
4. Choose appropriate $\delta \leq g(\epsilon)$
5. Work $|x - a| < g(\epsilon)$ forward to $0 < |f(x) - L| < \epsilon$ form

2.3 Techniques for $\lim$ as $x \rightarrow a$

Basic Theorems

Basic substitution

Algebraic specials: factoring/reducing; addition, rationalization of numerator

Proof of “Limit of sum = sum of limits” (supply pieces or reasons only)

Triangle inequality

Sandwich theorem pp. 64-65 do Thursday 2/16

2.4 Limits involving ∞

Limits at ∞ ($\pm \infty$) as $x \rightarrow a$

Limits as $x \rightarrow \pm \infty$

2.5 Continuity

Definition of $f(x)$ being continuous at c if three conditions are met:

- 1) $f(c)$ is defined (not $\pm \infty$ or division by zero or $\sqrt{\text{ of negatives, etc.)}$
- 2) $\lim f(x)$ exists as $x \rightarrow c$
- 3) $\lim f(x) = f(c)$ as $x \rightarrow c$

Theorem 2.21

Theorem 2.26 and do 55-58 Thursday 2/16